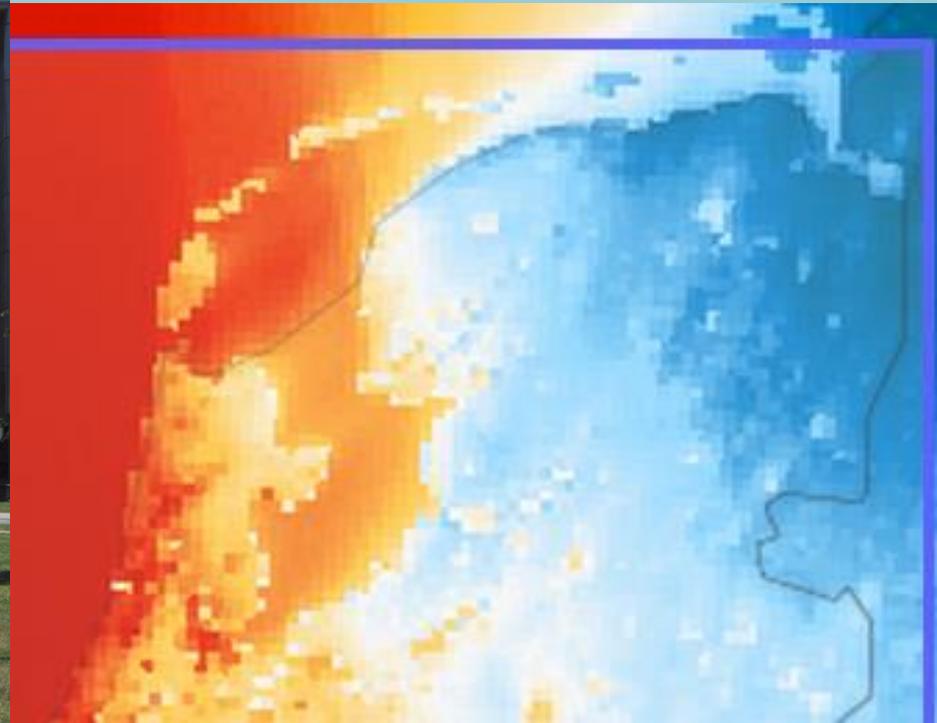




Koninklijk Nederlands
Meteorologisch Instituut
Ministerie van Infrastructuur en Milieu

High Resolution Temperature Interpolation

Marieke Dirksen





Importance of high resolution Temperature

- Insurance, environment, agriculture
- Input for hydrological models and others
- Understanding Temperature patterns of the past helps to understand the current and future Temperature patterns





KNMI meteorologische stations



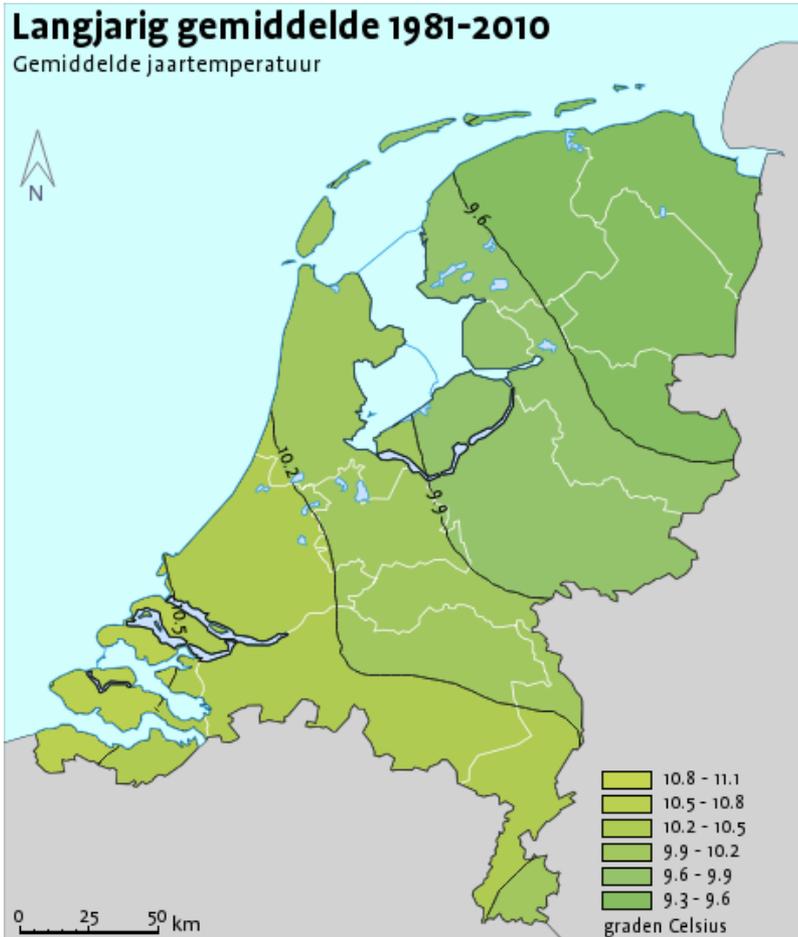
De Bilt



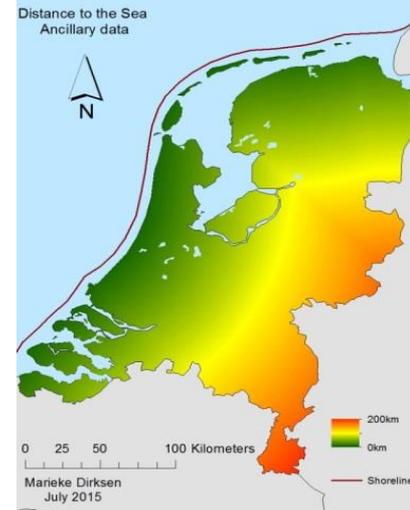
(c) 2014, KNMI Klimaatdata en advies



Current Interpolation: with distance to the sea



- 33 Observations
- Trend: Distance to sea
- Kriging interpolation



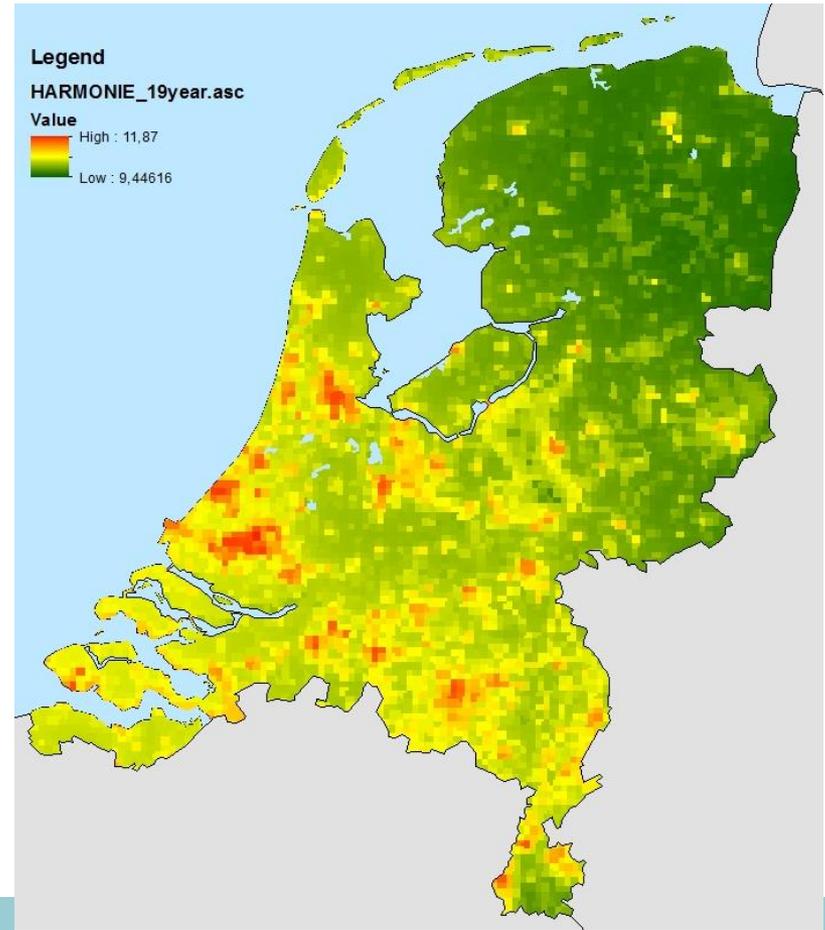
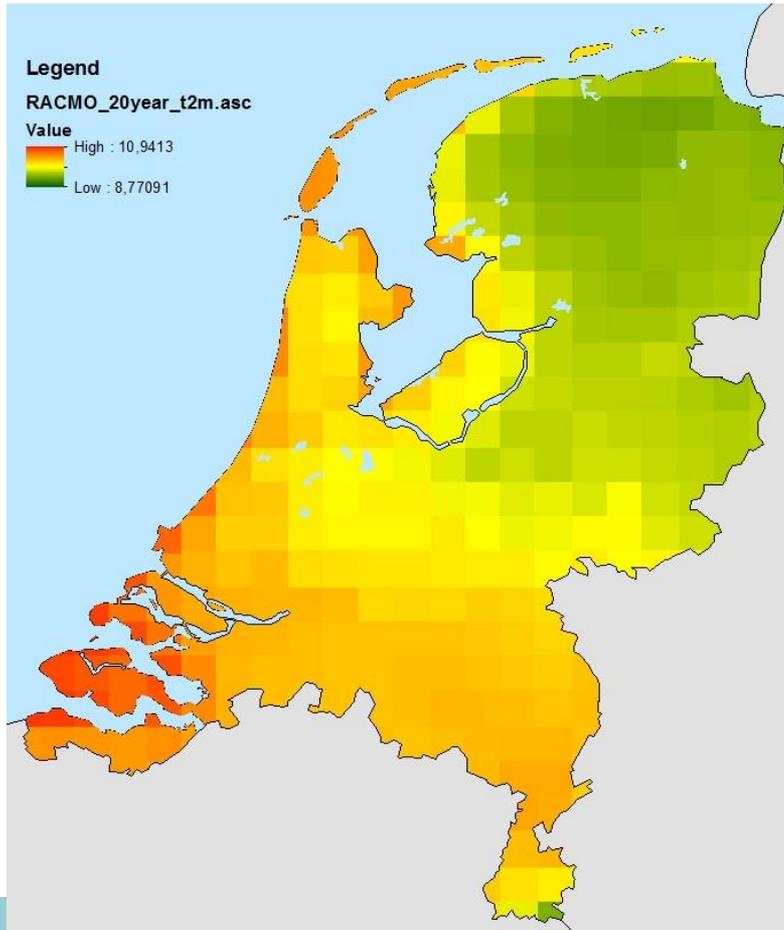


Numeric Weather Prediction model data

RACMO (12km grids)

&

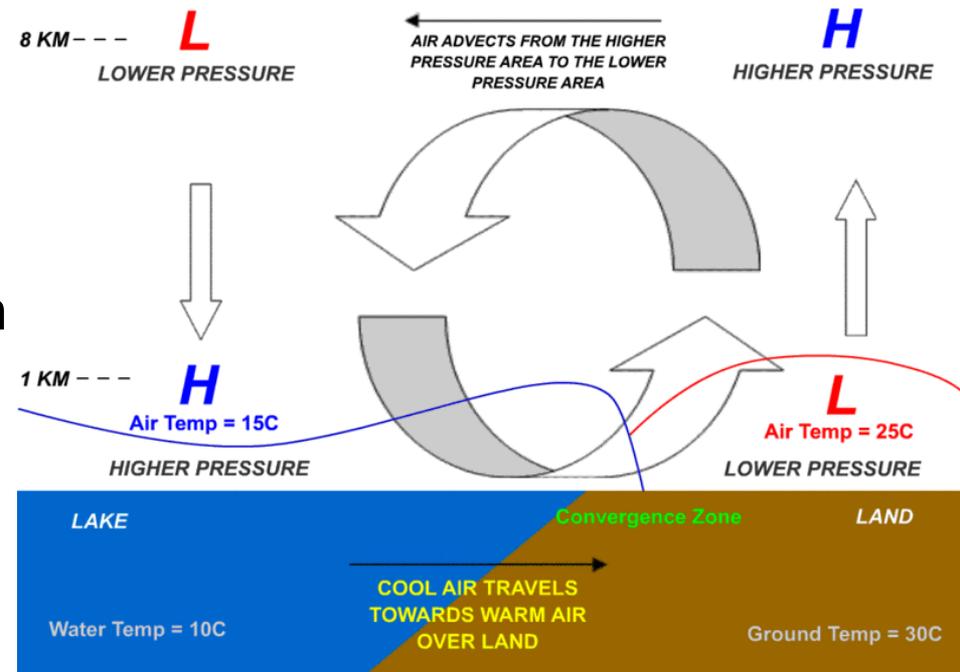
HARMONIE (2.5km grids)





Combining observation and NWP model trend

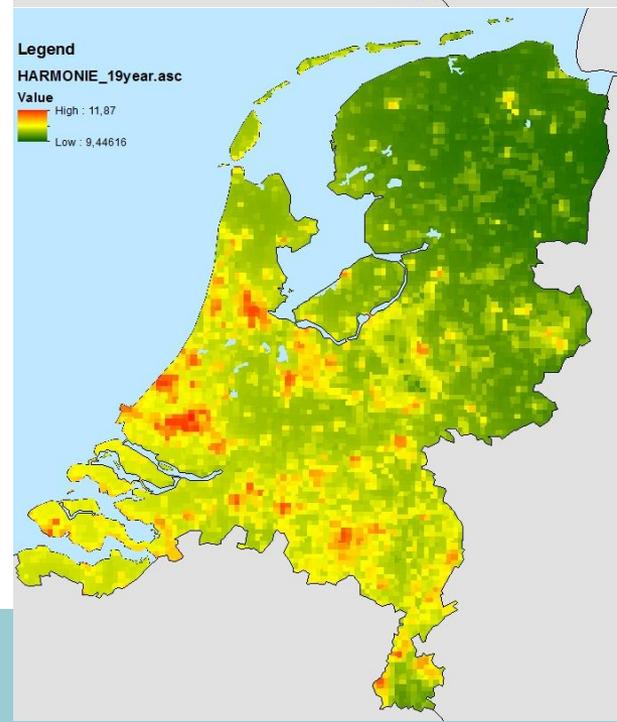
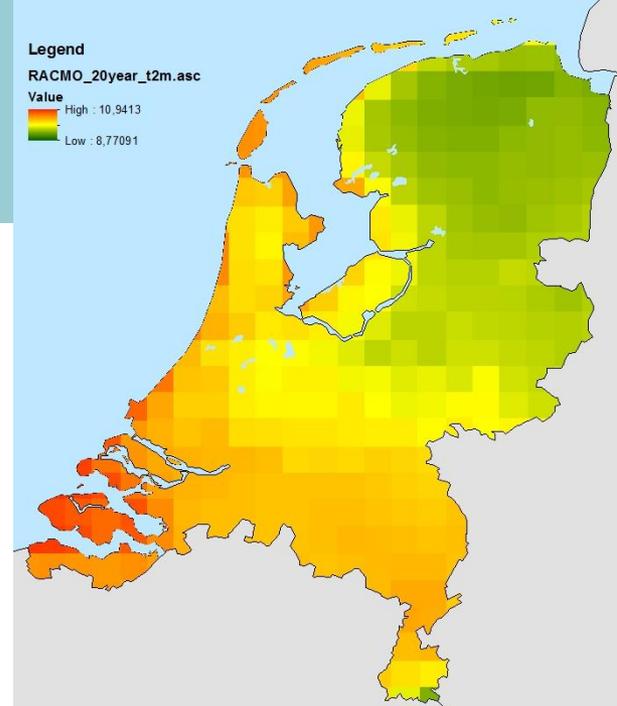
- 33 observations=limited
- Large scale patterns: Land surface atmosphere interaction
- Included in models
- Use model trend for interpolation





Data Analysis: an example

- Period: 20 years, from 1995-2014
- Observations: 33 stations
- NWP models: RACMO & HARMONIE
- Interpolation method: Universal Kriging with an exponential variogram model
- Output: 1x1km Temperature grid



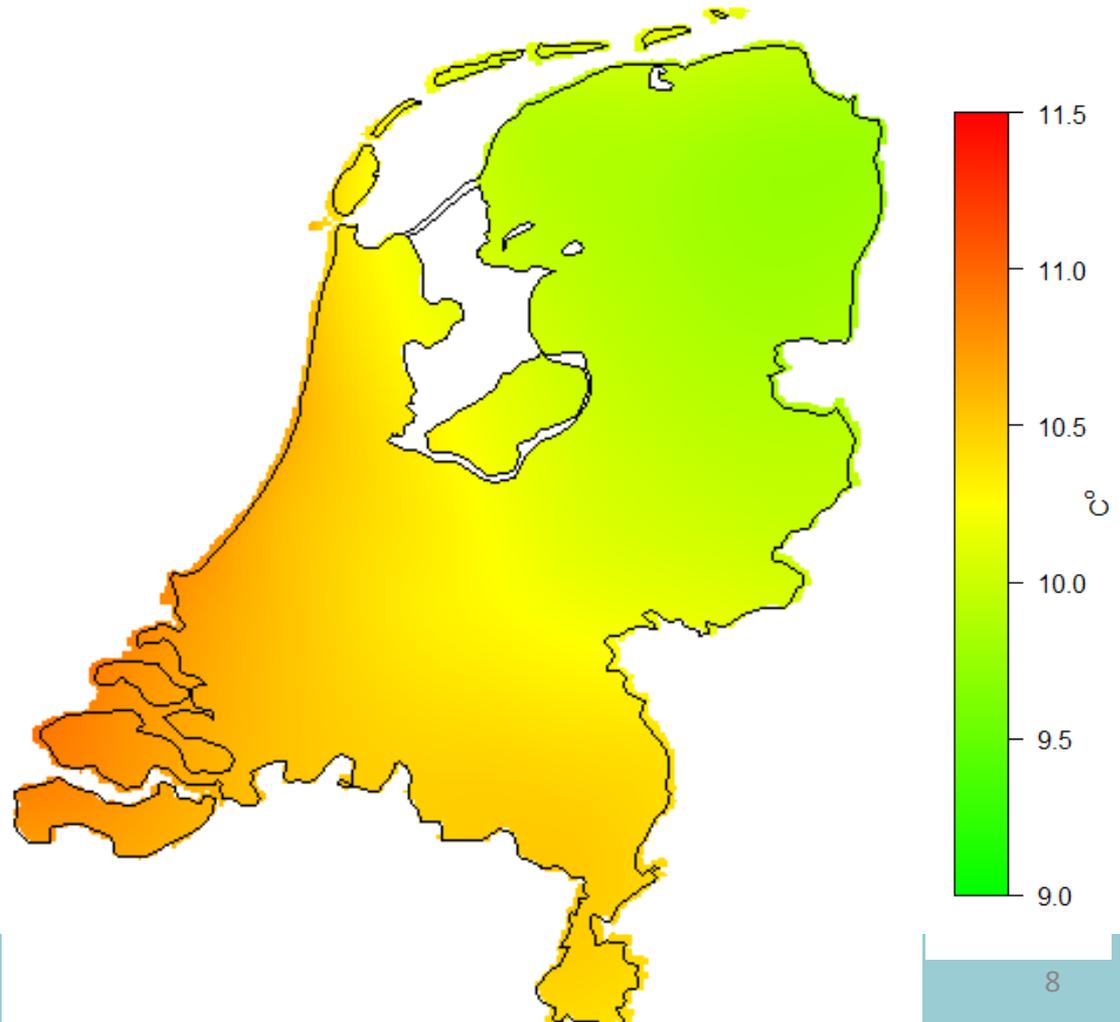


Observations & trend Distance to the Sea

LOOCV

$R^2=0.76$

RMSE=0.012



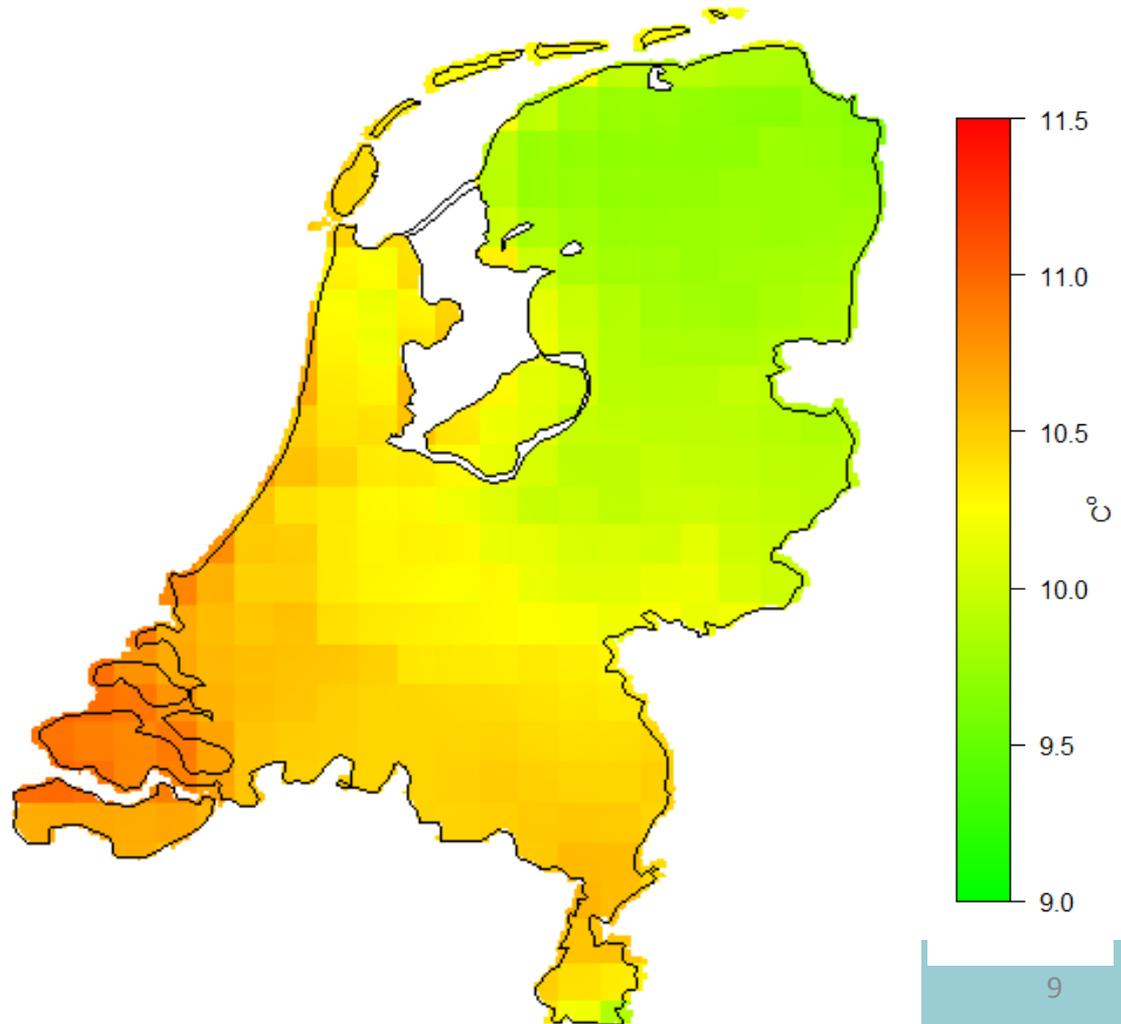


Observations & trend RACMO Temperature Grid

LOOCV

$R^2=0.79$

RMSE=0.037



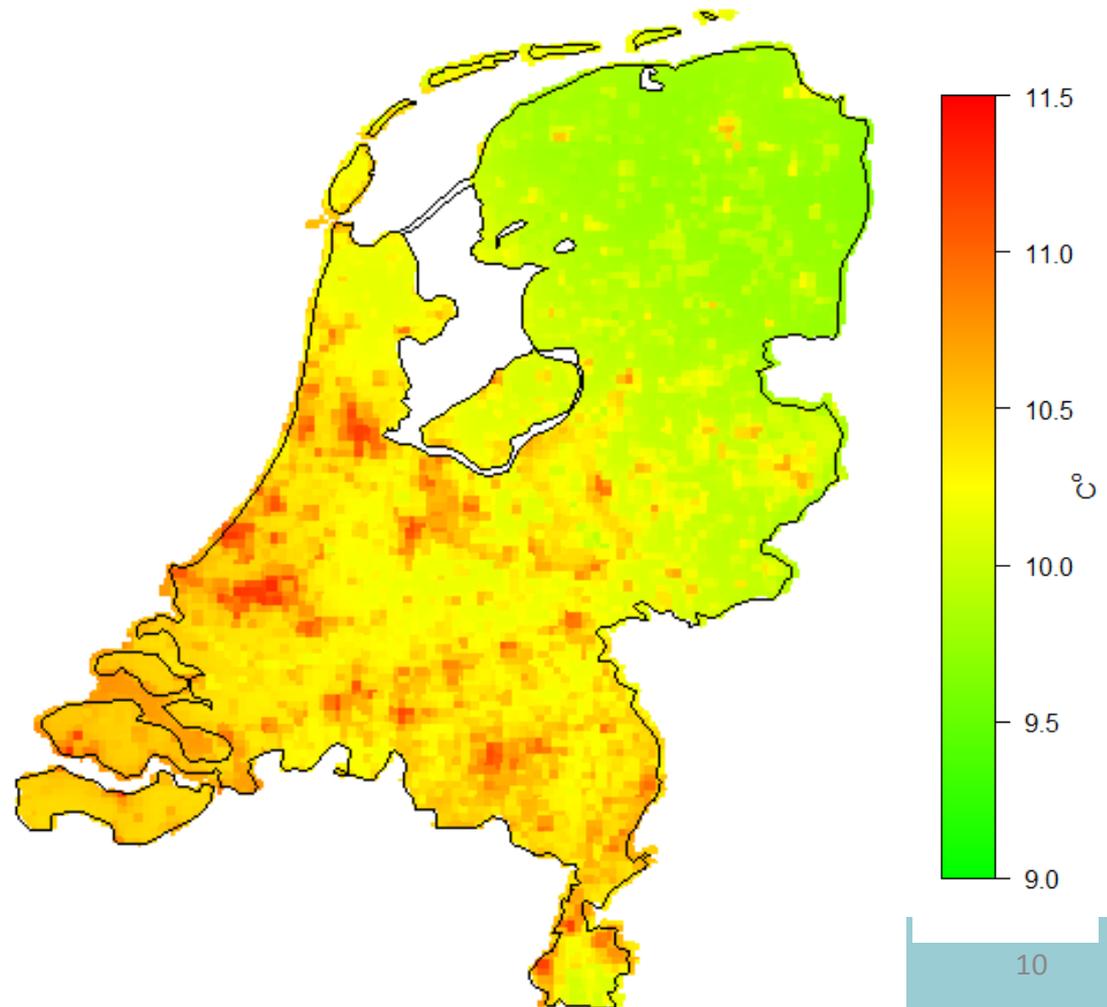


Observation & trend HARMONIE Temperature Grid

LOOCV

$R^2=0.79$

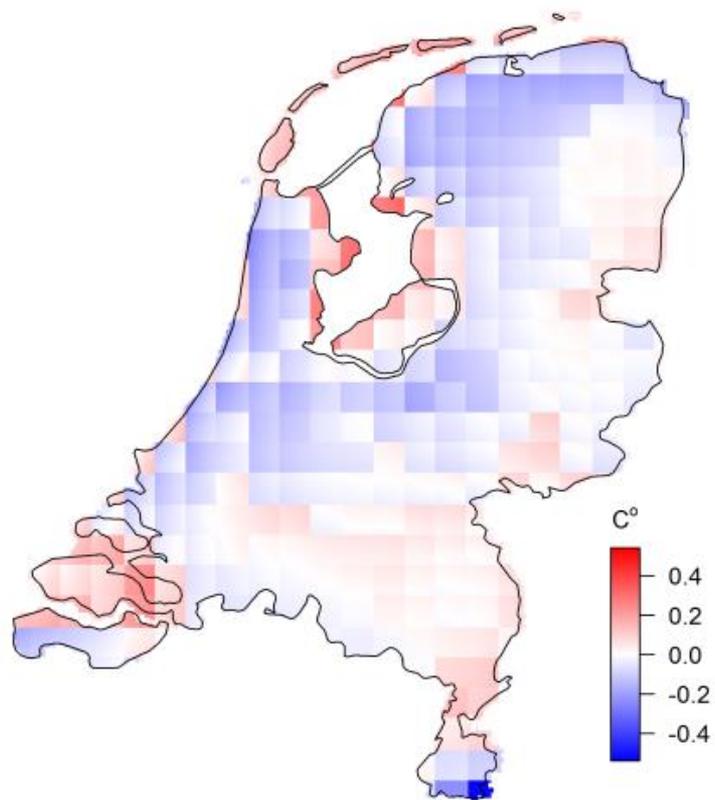
RMSE=0.150



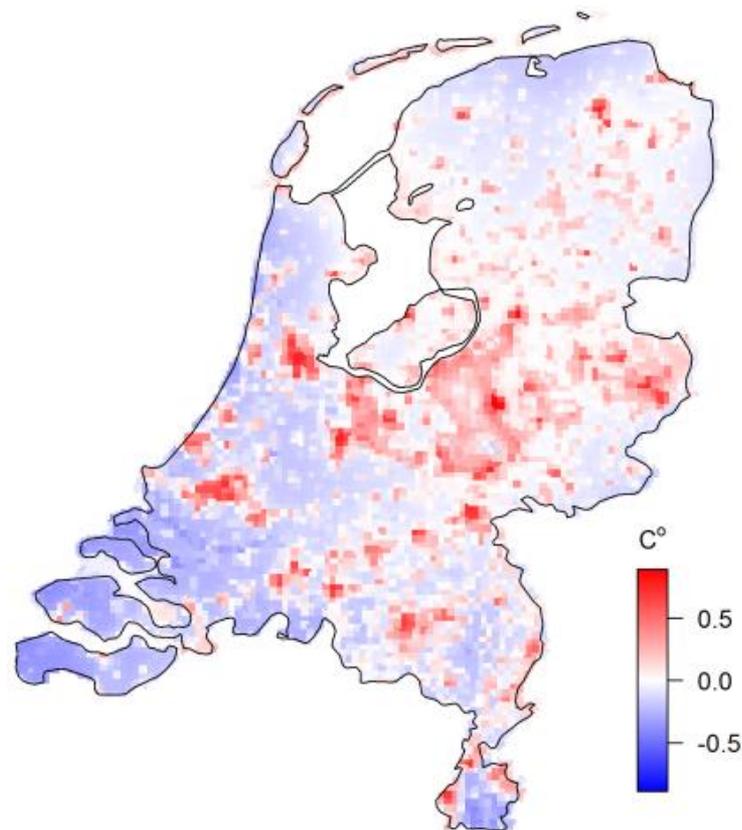


Differences

RACMO-distance sea



HARMONIE-distance sea





Case Example: Daily interpolation

- Period: day 2010/01/01
- Observations: 33 stations
- NWP models: RACMO & HARMONIE
- Interpolation method: Universal Kriging with an exponential variogram model
- Output: 1x1km Temperature grid

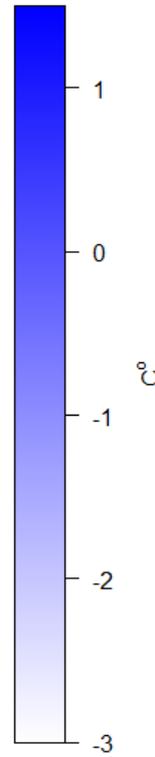
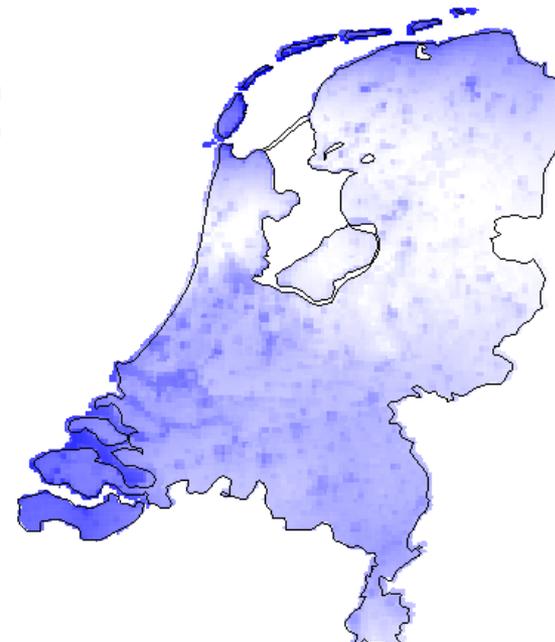
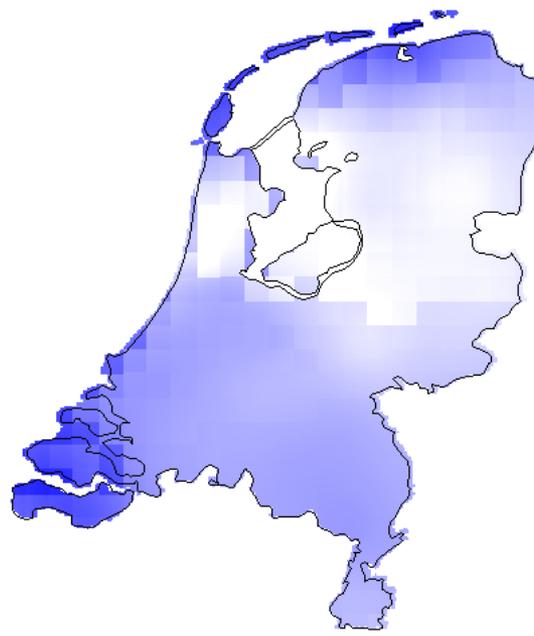


Daily interpolation: 2010/01/01

Observation

RACMO

HARMONIE



R2=0.65
RMSE=0.036

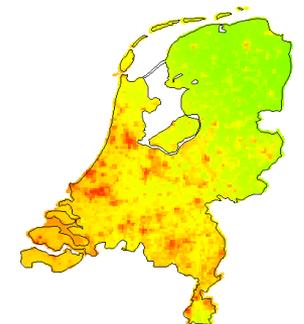
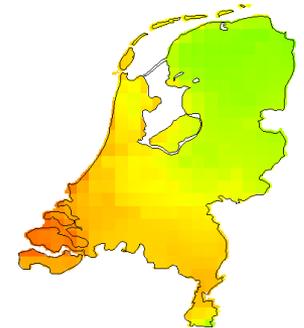
R2=0.50
RMSE=0.088

R2=0.73
RMSE=0.0057



Conclusion

- Statistically good correlations (R^2 , RMSE), shorter time periods interpolation with model data preferred
- Including NWP model data: better spatial patterns
- Cities & elevated area's can be recognized when using HARMONIE





Questions?



Additional slides

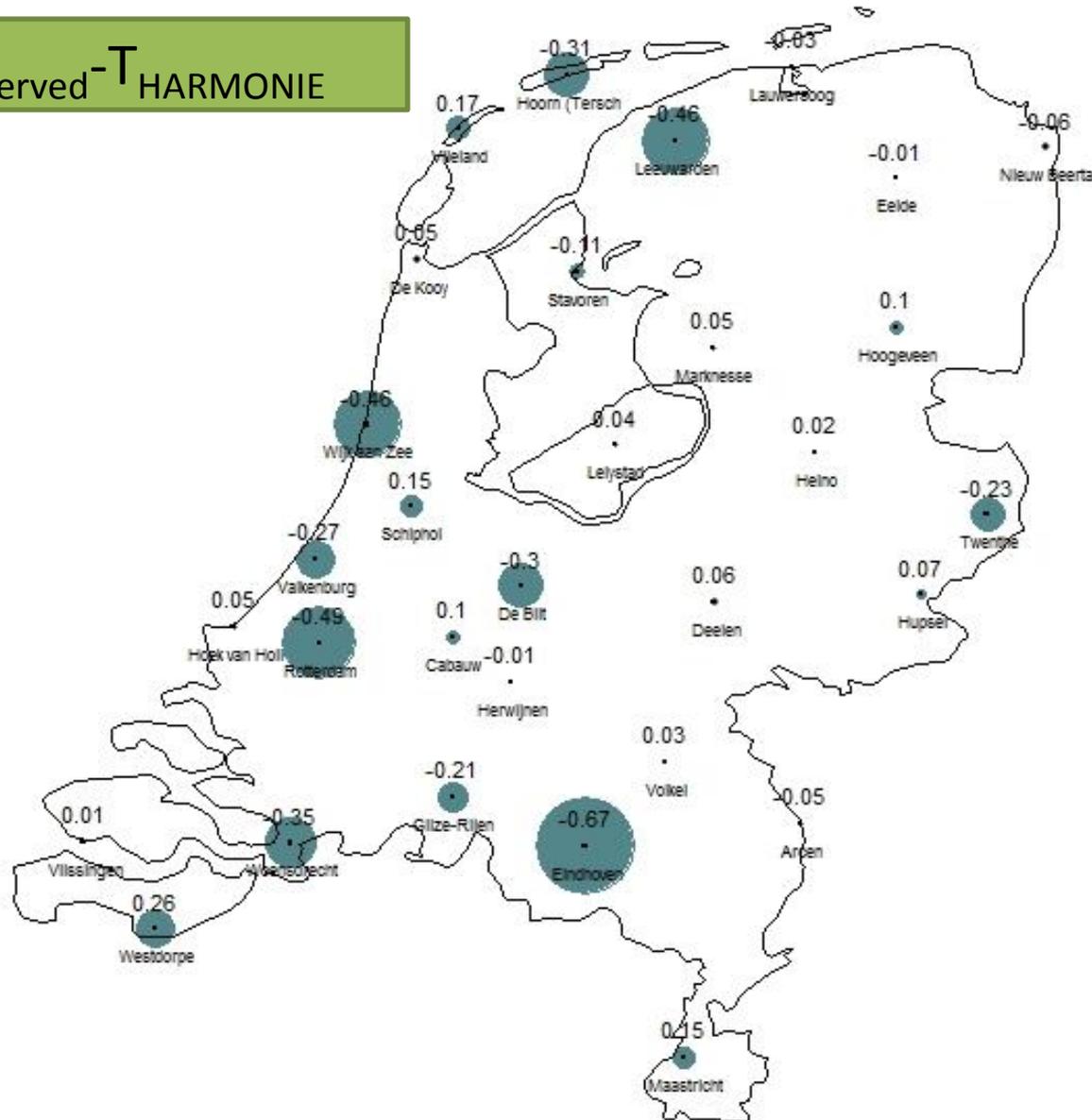
- Comparison: RACMO & HARMONIE 20 year difference
- Comparison: models RACMO & HARMONIE vs. observations
- Daily interpolation (cold day)
- 20 year monthly (September)
- Background Kriging

In general, it can be observed that when the time period decreases R^2 decreases and RMSE increases

Temperature difference HARMONIE and Observations

$$T_{\text{diff}} = T_{\text{observed}} - T_{\text{HARMONIE}}$$

-0.087



Overview of the data analysis

Variables

Mean Temperature
Maximum Temperature
Minimum Temperature

Time

Day
Month
Year
20 year (including 20 year monthly average)

Interpolation

Ordinary Kriging
Universal Kriging
TPS
IDW

Ancillary data

RACMO
HARMONIE
Distance to the sea

Validation

Cross validation
Point difference (observation vs. prediction)
Variance maps

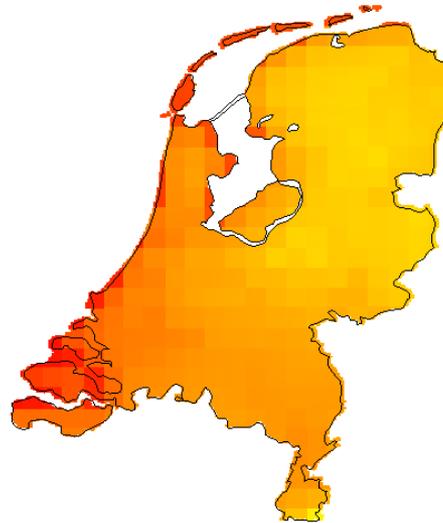
20year month: September

Klimaatatlas



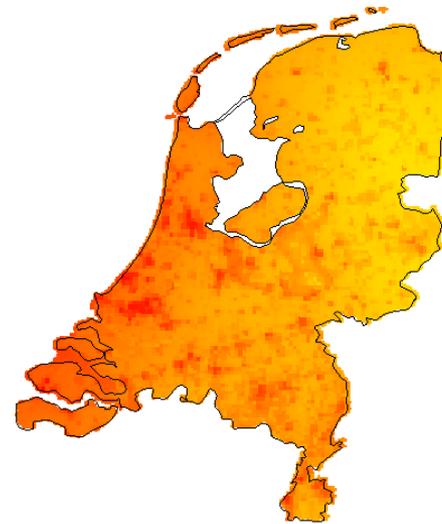
R2=0.71
RMSE=0.032

RACMO

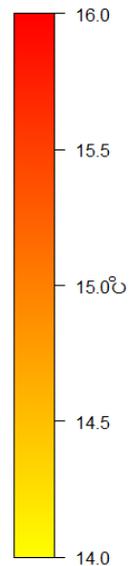


R2=0.82
RMSE=0.033

HARMONIE

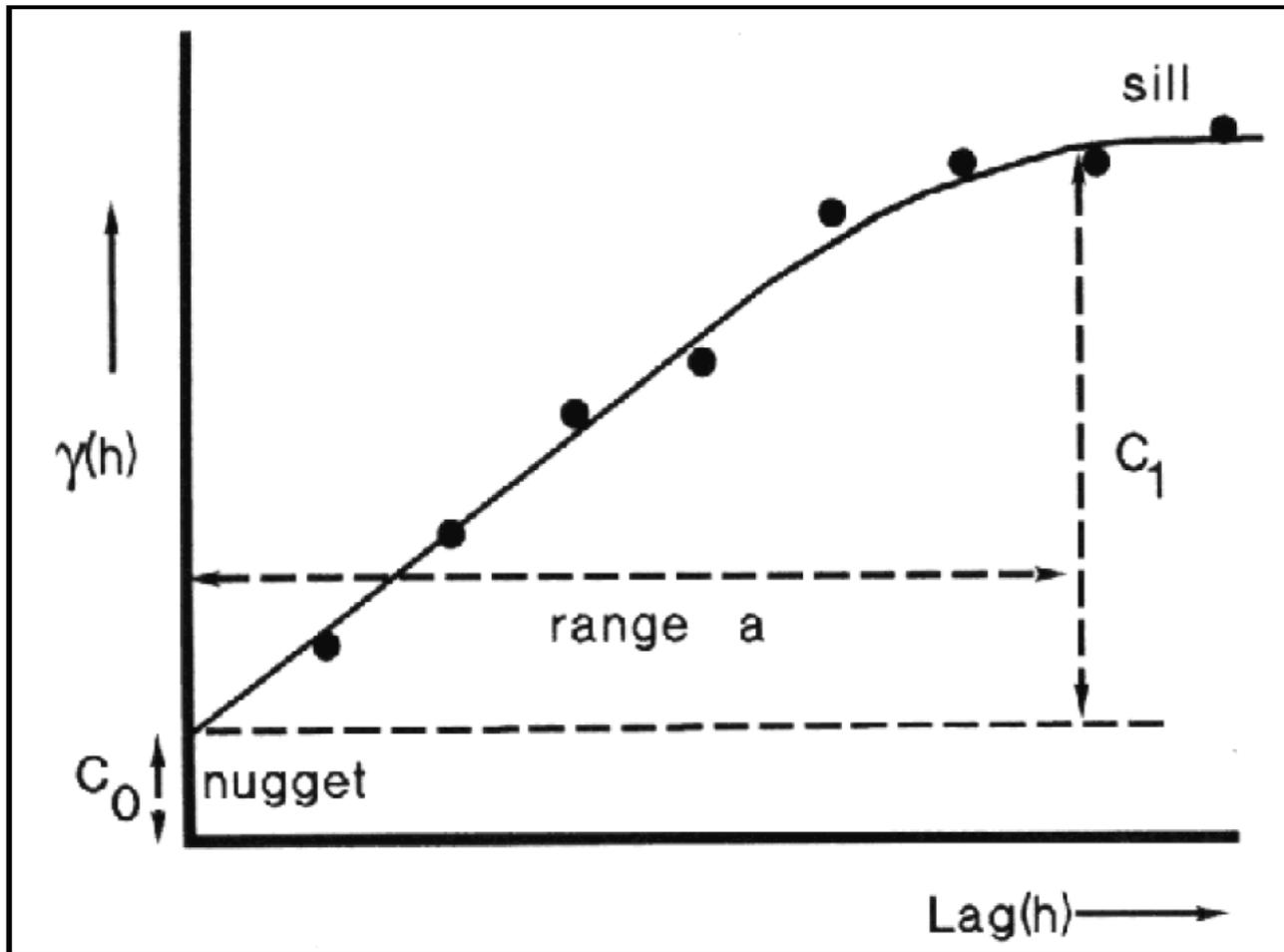


R2=0.56
RMSE=0.015



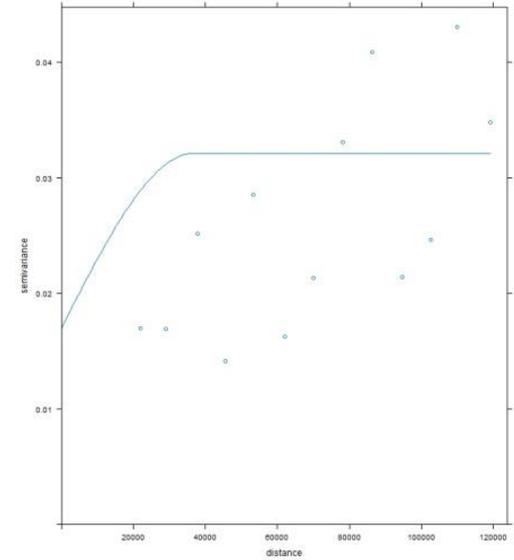
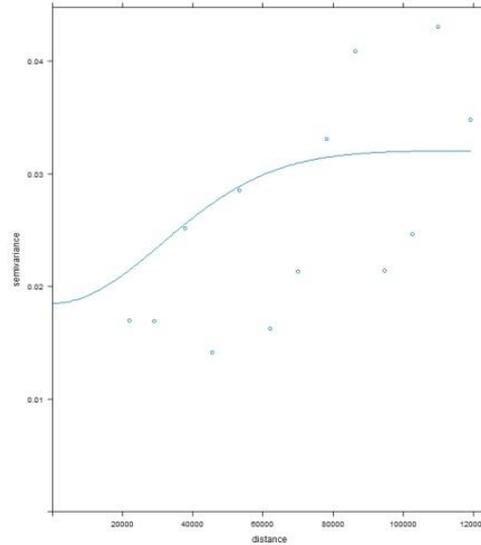
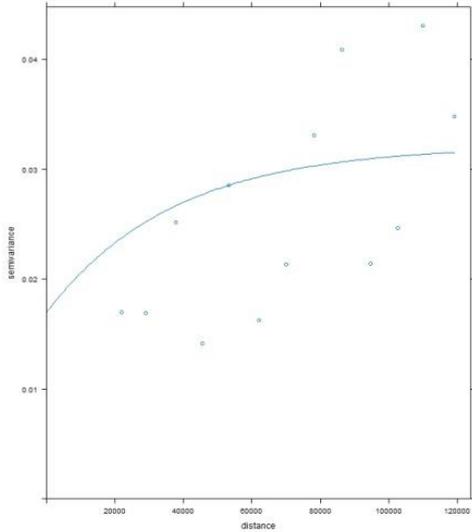
Kriging: the basics

- Similar idea as IDW ($w(x_i) = \|x_i - x_0\|^{-p}$)
- Residuals are spatially correlated and represented by the covariance
- Below an example of a variogram model:



Variogram fits

Exponential, Gaussian and spherical models, RACMO 20 year t2m



Interpolation method	SSERR
OKexp	3.9e-11
OKsph	1.2e-10
KEDexpS	3.4e-11
KEDsphS	9.5e-11
KEDgauS	2.1e-11
KEDexplS	1.9e-11
KEDsphLS	3.0e-11
KEDgauLS	8.0e-11
KEDexpR	3.1e-12
KEDsphR	8.2e-12
KEDgauR	2.5e-12

KED RACMO	Nugget	Sill	Range
Exponential	0.0169	0.0321	36894
Gaussian	0.0185	0.0321	44273
Spherical	0.0169	0.0321	36894

Kriging Interpolation in R

Example of universal kriging with an exponential variogram model:

```
ked_exp <- autoKrige(Tg_new~distshore, var, distshore.grd,  
maxdist=mxdkrige, block=c(blocksize,blocksize), model = c("Exp"),  
na.action=na.pass, fix.values=c(NA,NA,NA), miscFitOptions =  
list(merge.small.bins = TRUE))
```

Notice:

- The model depends on ancillary data (~distshore)*
- The temperature observations (Tg_new from var) are interpolated over a grid (distshore.grd)*
- For the variogram a maximum distance, blocksize and model is chosen*
- For a complete analysis not only the model is (Exp, Sph, Gauss) is adapted but also maxdist and block!*

Cross-validation in R

By means of e.g. cross-validation the performance of different interpolation methods can be assessed (Hiemstra & Sluiter, 2011). Below an example for the cross validation for Kriging:

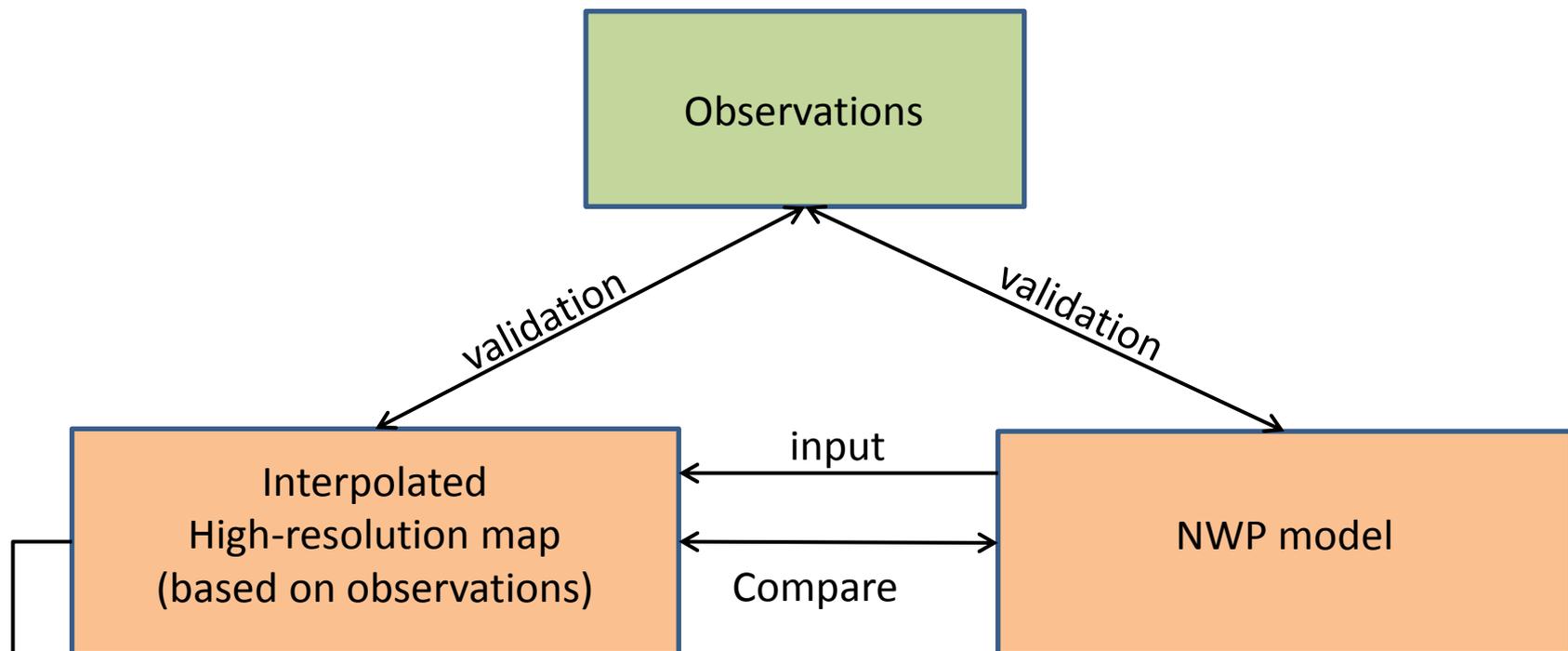
```
ked_exp.cv<-autoKrige.cv(Tg_new~distshore,var,model=c("Exp"), maxdist=mxdkrige,  
fix.values=c(NA,NA,NA), miscFitOptions = list(merge.small.bins = TRUE))
```

Input: same variables as in autokrige!

Output: spatial data frame with LOOCV



Overview of the data analysis in R



- Available interpolation methods
- New interpolation methods
- Comparison and improvement